

Sub-millimeter and Millimeter Detection

$$0.2 \text{ mm} \lesssim \lambda \lesssim 3 \text{ mm}$$

photon energies $\sim 10 \text{ meV} - 10 \text{ meV}$

photon detector - nonthermal distribution of excited electrons

thermal detector - excitations from photons have relaxed to a thermal distribution before detection

Use thermal detectors

Still incoherently measuring incident power

Associated instrumentation is similar to CCD's (UV, optical, IR), but some material properties make optical elements different ~~(same)~~ (same design principles)

E.g. mirror surface accuracy requirements

scale $\propto \lambda$, so finish can be $\sim \frac{10^{-3}}{5000 \times 10^{-9}} \sim 1000 \times$ rougher
finely polished, plated glass vs. machined surface

Atmospheric absorption lines are extremely important for ground-based observations

Atmospheric "windows" define commonly used bands

Water, oxygen absorb in these wavelengths

Scale height of atmospheric gases $\sim 8 \text{ km}$ ($1/e$)

Scale height of water $\sim 2 \text{ km}$

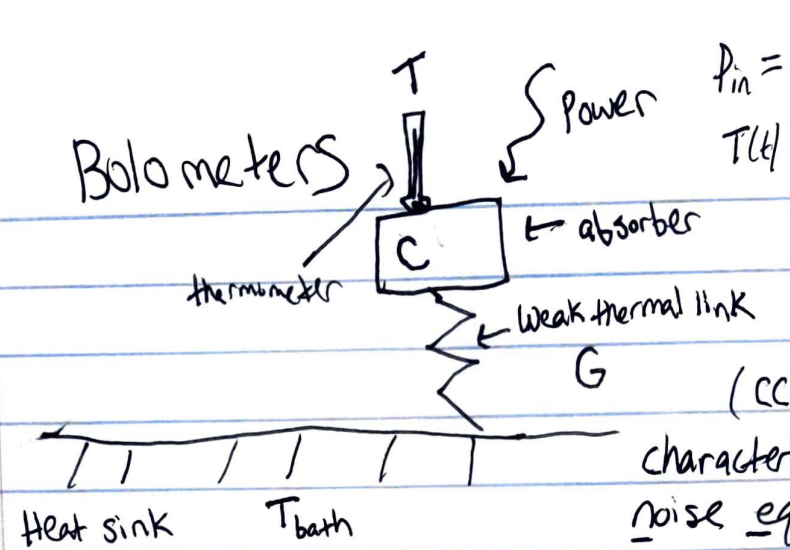
Residual water ~~effects~~ efficiency and noise (sort of like light pollution)

Atmospheric "seeing" is also important

Water is "bright", but sun and moon are dim in mm-wave

Can observe any time weather is good (daytime, full moon)

$$\dot{Q} = \frac{dP}{dT}$$



$$P_{in} = P_0 + \eta P_i(t) = GT + C \frac{dT}{dt}$$

$$T(t) = \begin{cases} P_0/G, & t < 0 \\ P_0/G + \frac{\eta P_i}{G} (1 - e^{-t/(C/G)}) & t \geq 0 \end{cases}$$

Temperature rise \propto incoming power
read out thermometer

(CCDs had signal proportional to # of photons)
characterize noise with NEP
noise equivalent power

speed of bolometer response $\tau_{thermal} = \frac{C}{G}$

fundamental noise source (fluctuations on thermal link)
NEP_{phonon thermal} = $\sqrt{4KT^2G}$

NEP: power on detector with S/N of 1 (in 1 Hz bandwidth)
how small of a power can you detect (lower is good)

NEP_{thermal} $\propto T, \sqrt{G}$ want it to be cold, with a very weak thermal link

little G slows down detector, and can cause it to "saturate,"
so need to carefully tune parameters

also NEP_{photon} = $\frac{hc}{\lambda} \left(\frac{2\Phi}{\eta}\right)^{1/2}$ (Φ = photons/s) (noise $\propto \sqrt{N}$)

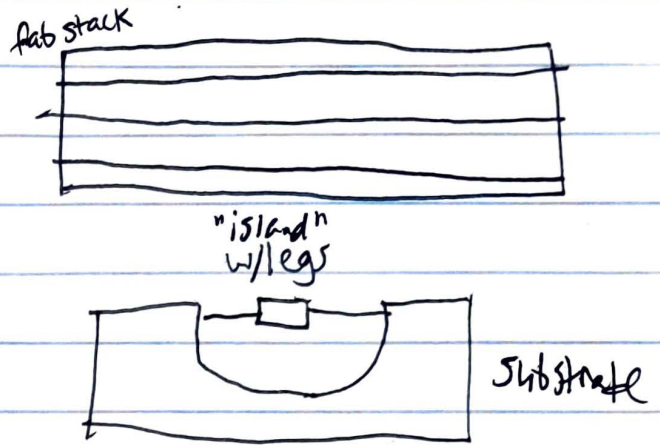
Detector is sensitive to all incident power, including atmosphere, optics, etc, so have to carefully filter for desired signal, and keep instrument as cold as possible (blackbody radiation)

Want photon-noise limited performance ($NEP_{photon} \gg NEP_{phonon}$)
(ideally almost all signal-photons contributing to NEP_{photon})

From best ground sites, need $T \approx 300$ mK

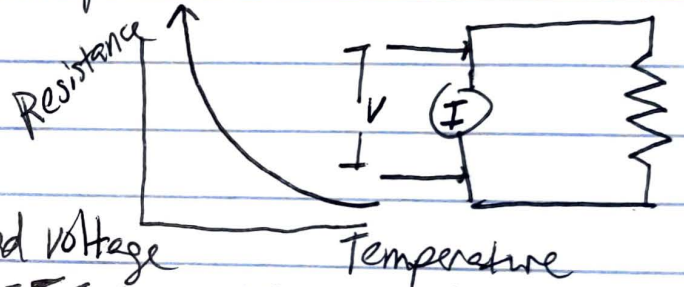
From balloons and space, need $T \approx 100$ mK

Bolometer structure is created w/ "silicon micromachining"
 $\sim < 1 \text{ mm}$ pixel dimension
photolithography



How to read out temperature?

- use doped silicon
- strong R vs T
- bias w/ current and read voltage
- use a JFET or MOSFET amplifier, to amplify voltages
- make resistance high (high-impedance amplifiers)



used on Herschel / PACS (2048-pixel array)

P_{bias} electrical power to measure resistance
 current bias: constant current

$$P_{\text{bias}} = I_{\text{bias}}^2 R, \quad V = I_{\text{bias}} \cdot R$$

dR/dT is negative

incoming Power $\Rightarrow T \uparrow, R \downarrow$, and $P_{\text{bias}} \downarrow$

$P_{\text{opt}} \uparrow, P_{\text{bias}} \downarrow$ negative feedback
 electro thermal feedback

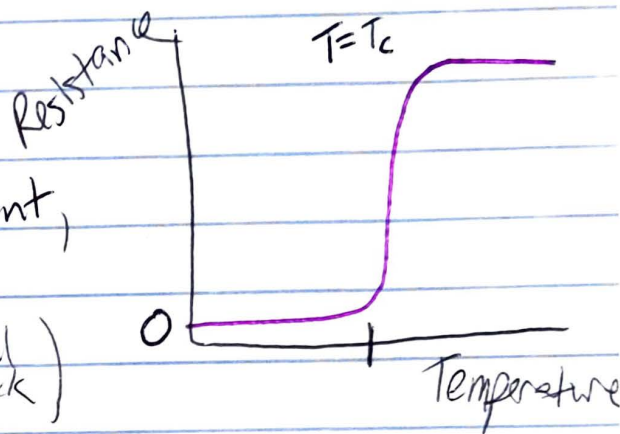
dR/dT sets strength of feedback

want high dR/dT for strong feedback

strongest known temperature dependence is in superconducting transition

$$dR/dT > 0$$

If biased with constant current, feedback is positive unstable (w/o external feedback)



Need to cool to superconductor's critical temp, but already driven to low temp by fundamental noise sources

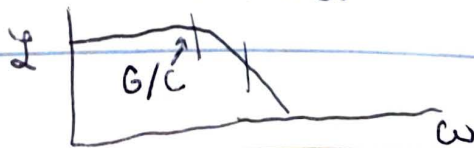
To get negative electrothermal feedback, need to voltage bias (easier said than done)

$$P_b = \frac{V_b^2}{R} \quad \frac{dP_b}{dT} = -\frac{V_b^2}{R^2} \frac{dR}{dT} < 0$$

With time-varying optical signal $\delta P_{opt} e^{i\omega t}$ define loop gain \mathcal{L}

$$\mathcal{L}(\omega) = \frac{-\delta P_{bias}}{\delta P}$$

$$\mathcal{L}(\omega) = \frac{\mathcal{L}}{1 + i\omega T_0} \quad T_0 = \mathcal{L}/G$$



Actually measuring current I
responsivity is $S_{\pm} = \frac{dI}{dP_{opt}}$

$$S_{\pm} = -\frac{1}{V_{bias}} \frac{Q}{Q+1} \frac{1}{1+i\omega\tau} \Rightarrow -\frac{1}{V_b} (Q \gg 1)$$

$$\tau = -\frac{\tau_0}{Q+1}$$

Achievable Q set by $\frac{dR}{dT}$

(TES)

$Q \gg 1$ only possible w/ superconducting transition
negative electrothermal feedback w/ $Q \gg 1$

only possible w/ voltage-biased superconducting transition

want linear responsivity, independent of
 P_{opt} , T_{lath}

How to read out current? $R \sim$ few ohms, at most
- need a low impedance amplifier

breakthrough in TES usability w/ use of SQUIDS

Superconducting ~~QED~~ Quantum Interference Device

extremely sensitive magnetometers

Josephson junction: insulator separating two superconductors
superconducting Cooper pairs of electrons tunnel through

SQUID: two JJ's in superconducting loop

amount of flux in loop is quantized

develops a voltage proportional to flux (induced by I)

read out voltage w/ good amplifier

